

# Mathematical modeling of a dynamic thin plate deformation in acoustoelasticity problems

Badriev I., Paimuhin V.

Kazan Federal University, 420008, Kremlevskaya 18, Kazan, Russia

---

## Abstract

© Published under licence by IOP Publishing Ltd. The coupled problem of planar acoustic wave propagation through a composite plate covered with a second damping layer with a large logarithmic decrement of oscillations is formulated. The aerohydrodynamic interaction of a plate with external acoustic environment is described by three-dimensional wave equations and the mechanical behavior of a two-layer plate by the classical Kirchhoff-Love model. An exact analytic solution of the problem is found for the case of hinged support of the edges of a plate. On the basis of this, the parameters of the covering damping layer were found, under which it is possible to achieve a practically complete damping of the plate vibration under resonant modes of its acoustic loading.

<http://dx.doi.org/10.1088/1755-1315/107/1/012095>

---

## References

- [1] Aureli M, Basaran M E and Porfiri M 2012 Nonlinear finite amplitude vibrations of sharp-edged beams in viscous fluids *Journal of Sound and Vibration* 331 54
- [2] Badriev I B, Makarov M V and Paimushin V N 2015 On the interaction of composite plate having a vibration-absorbing covering with incident acoustic wave *Russian Mathematics* 59 66-71
- [3] Gorshkov A G, Morozov V I, Ponomarev A T and Shklyarchuk F N 2000 *Aerohydroelasticity of structures* (Moscow: Fizmatlit) (in Russian)
- [4] Paimushin V N 2014 Dynamic instability of a compressible plate surrounded by an acoustic medium on free surfaces *Doklady Physics* 59 158-62
- [5] Badriev I B, Makarov M V and Paimushin V N 2015 Solvability of a physically and geometrically nonlinear problem of the theory of sandwich plates with transversal-soft core *Russian Mathematics* 59 57-60
- [6] Badriev I B, Makarov M V and Paimushin V N 2016 Mathematical Simulation of Nonlinear Problem of Three-point Composite Sample Bending Test *Procedia Engineering* 150 62
- [7] Sultanov L U and Davydov R L 2013 Numerical analysis of large deformation by finite element method *Magazine of Civil Engineering* 44 64-8
- [8] Badriev I B, Makarov M V and Paimushin V N 2016 Numerical Investigation of Physically Nonlinear Problem of Sandwich Plate Bending *Procedia Engineering* 150 5
- [9] Sultanov L U 2016 Analysis of finite elasto-plastic strains. Medium kinematics and constitutive equations *Lobachevskii Journal of Mathematics* 37 787-93
- [10] Badriev I B, Makarov M V and Paimushin V N 2017 Contact statement of mechanical problems of reinforced on a contour sandwich plates with transversally-soft core *Russian Mathematics* 61 69-75
- [11] Badriev I B, Garipova G Z, Makarov M V, Paimushin V N and Khabibullin R F 2015 Solving Physically Nonlinear Equilibrium Problems for Sandwich Plates with a Transversally Soft Core *Lobachevskii Journal of Mathematics* 36 474-81
- [12] Moon S I and Jang J J 1999 The effect of polybutadiene interlayer on interfacial adhesion and impact properties in oxygen-plasma-treated UHMPE fiber/epoxy composites *Composites. Part A* 30 44

- [13] Kudinov V V, Shaekhov M F and Korneeva N V 2004 Effect of Plasma Treatment and Impregnation Technology on the Joint Strength of Epoxy Matrix with a Polyethylene Fiber during the the Production of Composite Materials *Fiz. Khim. Obrab. Mater.* 3 24
- [14] Sergeeva E A 2010 Effect of plasma treatment on the structure and properties of high-modulus polyethylene fibers *Voprosyi materialovedeniya* 2 51-7 (in Russian)
- [15] Panovko Ya G 1960 Internal friction in the case of vibrations of elastic systems (Moscow: Fizmatgiz) (in Russian)
- [16] Khilchevsky V V and Dubenets V G 1977 Scattering of energy in vibrations of thin-walled structural elements (Kiev: Vischa shkola) (in Russian)
- [17] Gazizullin R K and Paimushin V N 2016 The transmission of an acoustic wave through a rectangular plate between barriers *Journal of applied mathematics and mechanics* 80 421-32
- [18] Paimushin V N 2015 Sound-wave passage through a composite plate with a vibration-absorbing surface *Doklady physics* 60 263-8
- [19] Paimushin V N 2014 On the Problems of Emission of Sound Waves in the Dynamic Process of Deformation of Plates with Regard for External and Internal Damping *Journal of Mathematical Sciences* 203 87-103
- [20] Paimushin V N, Tarlakovskii D V, Gazizullin R K 2016 A Investigation of Different Versions of Formulation of the Problem of Soundproofing of Rectangular Plates Surrounded with Acoustic Media *Journal of Mathematical Sciences* 203 87-103
- [21] Badriev I B, Makarov M V and Paimushin V N 2015 On the interaction of composite plate having a vibration-absorbing covering with incident acoustic wave *Russian Mathematics* 59 66-71
- [22] Paimushin V N, Firsov V A, Gyunal I and Egorov A G 2014 Theoretical-Experimental Method for Determining the Parameters of Damping Based on the Study of Damped Flexural Vibrations of Test Specimens 1. Experimental Basis *Mechanics of composite materials* 50 127-36
- [23] Egorov A G, Kamalutdinov A M, Nuriev A N and Paimushin V N 2014 Theoretical-Experimental Method for Determining the Parameters of Damping Based on the Study of Damped Flexural Vibrations of Test Specimens 2. Aerodynamic Component of Damping *Mechanics of composite materials* 50 267-78
- [24] Paimushin V N, Firsov V A, Gyunal I, Egorov A G and Kayumov R A 2014 Theoretical-experimental method for determining the parameters of damping based on the study of damped flexural vibrations of test specimens. 3. Identification of the characteristics of internal damping *Mechanics of composite materials* 50 633-46